Homework DM II

Section 9.1: 3-9, 13, 16 Section 9.2: 1-5, 7-10, 18, 20, 20-25, 26, 28, 29, 30, 31, 32-35, 37, 47, 48, 49, 53*a*, 53*b*, 54-56 Section 9.3: 1, 3, 5, 7, 9, 10, 11, 13, 15, 19, 21, 23, 25, 28, 29, 32 (except *e*), 34-42, 46, 50-55 Graphical Sequences Problems: 4, 4, 4, 4, 4 1. 2. 2, 2, 2, 2, 2, 2 3. 3, 3, 3, 2, 2, 2, 2, 1 4. 4, 3, 1, 1, 1 5. 6, 4, 4, 3, 3, 2 6. 4, 4, 4, 4, 3, 2, 1, 1, 1 7. 4, 3, 3, 2, 2, 1, 1 8. 5, 3, 3, 2, 2, 2, 0 9. 5, 4, 4, 3, 1, 1, 1 10. 4, 4, 3, 3, 2, 2, 1, 1 11. 4, 4, 4, 3, 3, 3, 3, 2 12. 6, 5, 5, 4, 3, 3, 2, 2, 1, 1

- 13. Let *G* be a graph with $n \ge 2$ vertices and e = n 1 edges. Prove the existence of at least two vertices *u* and *v* such that $\deg(u) + \deg(v) \le 2$.
- 14. Determine, with proof, when the sequence of *n* 1's is graphical.
- 15. Determine, with proof, when the sequence of *n* 3's is graphical.

16. Determine, with proof, when the sequence of *n* 5's is graphical. Section 9.4: 1-6, 10-12, 18, 19, 21, 29-33, 37 Section 9.5: 1-10, 26, 27, 28, 30-40, 44, 45, 56-63 Section 9.7: 1-9, 12-14, 19-25 Section 9.8: 1-13, 15, 17-19, 21, 22 Find a graph *G* such that $\chi(G) = 4$ but *G* contains no triangles. Chromatic Polynomial handout: 1, 3, 7, 11-14 1. Can two non-isomorphic graphs have the same chromatic polynomial? Explain.