

**Review for Exam I**  
Calculus II sec. 001 Summer 2015

Sections Covered: 4.8, 5.2, 5.3, 5.4, 5.5, 5.6, 6.1

This practice exam is intended to give you a rough idea of the types of problems you can expect to encounter. **Nothing else is intended or implied.**

(1) Evaluate the given integrals.

(a) given  $\int_0^1 g(x) dx = 1$ , and  $\int_0^2 g(x) dx = 7$ , evaluate  $\int_1^2 g(x) dx$

(b)  $\int_{-1}^2 (x^2 + 3x - 1) dx$

(c)  $\int \tan^3 \frac{x}{2} \sec^2 \frac{x}{2} dx$

(d)  $\int_0^{\frac{\pi}{6}} \frac{\sin 2x}{\cos^4 2x} dx$

(e)  $\int_1^4 \frac{dy}{2\sqrt{y}(1 + \sqrt{y})^2}$

(f)  $\int \frac{x^3}{\sqrt{x^4 + 1}} dx$

(g)  $\int (\sec x - \csc(2x)) dx$

(h)  $\int_{-3}^{-1} \frac{x - 4}{x^2} dx$

(i)  $\int 3 \cot w dw$

(j)  $\int \left( \frac{1}{\sqrt{1 - x^2}} + \frac{2}{1 + 4x^2} \right) dx$

(k)  $\int \frac{2x + 1}{x^2 + x + 2} dx$

(2) Evaluate each integral by interpreting it in terms of areas.

(a)  $\int_0^4 -\sqrt{16 - x^2} dx$

(b)  $\int_0^2 f(x) dx$  where  $f(x) = \begin{cases} 1, & x \leq 1 \\ x, & x > 1 \end{cases}$

(3) Find the area bound between the indicated curves.

(a)  $x = 2y^2$ ,  $x = 0$ , and  $y = 3$ .

(b)  $y = \cos x$ ,  $y = \sin x$ , for  $0 \leq x \leq \frac{\pi}{2}$

(c)  $y = 2 - x^2$  and  $y = x$

(4) Evaluate each derivative.

(a)  $\frac{d}{dx} \int_x^{x^3} \tan t \, dt$

(b)  $\frac{d}{dx} \int_{\sin x}^{\cos x} \frac{dt}{t}$

(5) Explain why each statement below is false.

(a) If  $f$  is continuous on  $[a, b]$ , then

$$\frac{d}{dx} \left( \int_a^b f(x) \, dx \right) = f(x).$$

(b) If  $\int_0^1 f(x) \, dx = 0$ , then  $f(x) = 0$  for all  $0 \leq x \leq 1$ .

(c) If  $f$  is continuous on  $[a, b]$ , then  $f$  has a derivative on  $[a, b]$ .

(d) If  $f$  is continuous on  $[a, b]$ , then  $\int_a^b x f(x) \, dx = \frac{x^2}{2} \int_a^b f(x) \, dx$ .

(6) A particle moves along the  $x$ -axis; its acceleration  $a(t)$ , initial velocity  $v(0)$ , and initial position  $s(0)$  are given by

$$a(t) = 2 \cos t \text{ ft/s}^2, \quad v(0) = 2 \text{ ft/s}, \quad \text{and} \quad s(0) = 0 \text{ ft}.$$

Find the position  $s(t)$  for all  $t > 0$ .

(7) If  $f$  is continuous on  $[a, b]$  and  $m \leq f(x) \leq M$  on this interval, then  $m(b - a) \leq \int_a^b f(x) \, dx \leq M(b - a)$ . Use this property to show that

$$0 \leq \int_{-1}^{1/2} (1 - x^2) \, dx \leq \frac{3}{2}.$$