## Review for Exam 4

## MATH 1190

Sections Covered: 5.3, 5.4, 3.4, 4.1, 4.7

This review is provided as a courtesy to give some idea of what material is covered. Nothing else is intended or implied.
(1) The volume of a cube is increasing at a rate of $1200 \mathrm{~cm}^{3} / \mathrm{min}$ at the instant that its edges are 20 cm long? At what rate are the lengths of the edges changing at that instant?
(2) A stone dropped into a still pond sends out a circular ripple whose radius increases at a constant rate of $3 \mathrm{ft} / \mathrm{sec}$. How fast is the area enclosed by the ripple increasing at the end of 10 sec?
(3) A 10 foot ladder rests against a wall that makes a right angle with the ground. A person slides the base of the ladder away from the wall at a rate of $6 \mathrm{in} / \mathrm{sec}$. At the moment that the base is 6 feet from the wall, determine (a) the rate at which the top of the ladder is sliding down the wall, and (b) the rate at which the inclination angle between the base of the ladder and the ground is changing.
(4) Explain why each statement below is false.
(a) If $f$ is continuous on $[a, b]$, then

$$
\frac{d}{d x}\left(\int_{a}^{b} f(x) d x\right)=f(x)
$$

(b) If $\int_{0}^{1} f(x) d x=0$, then $f(x)=0$ for all $0 \leq x \leq 1$.
(c) If $f$ is continuous on $[a, b]$, then $f$ has a derivative on $[a, b]$.
(d) If $f$ is continuous on $[a, b]$, then $\int_{a}^{b} x f(x) d x=\frac{x^{2}}{2} \int_{a}^{b} f(x) d x$.
(5) Evaluate the given definite integrals.
(a) given $\int_{0}^{1} g(x) d x=1$, and $\int_{0}^{2} g(x) d x=7$, evaluate $\int_{1}^{2} g(x) d x$
(b) $\int_{-1}^{2}\left(x^{2}+3 x-1\right) d x$
(c) $\int_{0}^{\frac{\pi}{4}} \tan x \sec x d x$
(d) $\int_{0}^{\frac{\pi}{6}} \cos (r) d r$
(e) $\int_{0}^{1} \frac{2}{1+x^{2}} d x$
(f) $\quad \int_{-3}^{-2} \frac{1+x}{x} d x$
(g) $\int_{1}^{\ln 3} e^{x} d x$
(h) $\int_{1}^{4} \frac{x^{3}+8}{x^{2}} d x$
(i) $\int_{0}^{1}\left(x^{2}+1\right)^{2} d x$
(j) $\int_{-1}^{1} 2^{x} \ln (2) d x$
(6) Evaluate each derivative.
(a) $\frac{d}{d x} \int_{-1}^{x} \frac{\sin t}{t^{2}+1} d t$
(b) $\frac{d}{d x} \int_{x}^{2} t e^{t^{3}} d t$
(c) $\frac{d}{d x} \int_{1}^{\sqrt{x}} \tan \left(t^{2}\right) d t$
(d) $\frac{d}{d x} \int_{x}^{x^{2}} \sin ^{-1}(t) d t$
(7) Find the average value of the function over the indicated interval.
(a) $\quad f(x)=x^{2 / 3} \quad[-1,1]$
(b) $\quad f(x)=x+\cos x \quad[0, \pi]$
(c) $\quad f(x)=3^{x} \quad[0,2]$
(8) Find the point on the line $y=5 x+4$ that is closest to the origin.
(9) A grain silo in the shape of a right circular cylinder is to be mounted on a concrete slab. The lateral surface and top will be made out of steel. The silo must hold $8 \pi$ cubic meters of grain. Find the dimensions of the silo that will minimize the amount of steel used.
(10) A closed rectangular box with a square base is to be constructed. The material that the top and bottom (the square faces) are to be made of costs $\$ 2$ per square inch, and the material for the remaining four sides costs $\$ 1$ per square inch. If the box must have a volume of 16 cubic inches, determine the dimensions of the box that will minimize the cost of production.
(11) For each equation, identify a function whose root would be a solution to the equation. Set up Newton's Method for your function, and find $x_{1}$ using the given initial guess $x_{0}$.
(a) $\quad \cos x=x, \quad x_{0}=0$
(b) $\quad x^{3}=x+1, \quad x_{0}=1$

