Math 3322: Graph Theory¹

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Index of key terms

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This document (hopefully) includes all the key terms defined this semester, with the number of the lecture where it is defined. Sometimes, other lecture numbers are included in parentheses, for other lectures where the term comes up.

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¹This document comes from the Math 3322 course webpage: http://facultyweb.kennesaw.edu/mlavrov/courses/3322-fall-2023.php

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